

CLAIMS

Sub B³ 1. An encoder having means for calculating the DCT of a sequence of length $N/2$, N being a positive, even integer, **characterised by**

- means for calculating a DCT of length N directly from two sequences of length $N/2$ representing the first and second half of an original sequence of length N .

2. An encoder having means for calculating the DCT of a sequence of length $N/2 \times N/2$, N being a positive, even integer, **characterised by**

- means for calculating an $N \times N$ DCT directly from four DCTs of length $(N/2 \times N/2)$ representing the DCTs of four adjacent blocks constituting the $N \times N$ block.

A 3. An encoder according to ^{Claim 1} any of claims 1 or 2, **characterised in that** the means for calculating DCTs of length $N/2$ are arranged to calculate the even coefficients of a DCT of length N as:

$$\begin{aligned}
 X_{2k} &= \sqrt{\frac{2}{N}} \varepsilon_{2k} \sum_{n=0}^{N-1} x_n \cos \frac{(2n+1)2k\pi}{2N} \\
 &= \sqrt{\frac{2}{N}} \varepsilon_k \left\{ \sum_{n=0}^{\frac{N}{2}-1} x_n \cos \frac{(2n+1)k\pi}{2(N/2)} + \sum_{n=N/2}^{N-1} x_n \cos \frac{(2n+1)k\pi}{2(N/2)} \right\} \\
 &= \sqrt{\frac{2}{N}} \varepsilon_k \left\{ \sum_{n=0}^{\frac{N}{2}-1} y_n \cos \frac{(2n+1)k\pi}{2(N/2)} + \sum_{n=0}^{\frac{N}{2}-1} x_{N-1-n} \cos \left[\frac{[2(N-1-n)+1]k\pi}{2(N/2)} \right] \right\} \\
 &= \sqrt{\frac{1}{2}} \left\{ \sqrt{\frac{2}{N/2}} \varepsilon_k \sum_{n=0}^{\frac{N}{2}-1} y_n \cos \frac{(2n+1)k\pi}{2(N/2)} + \sqrt{\frac{2}{N/2}} \varepsilon_k \sum_{n=0}^{\frac{N}{2}-1} z_n \cos \frac{(2n+1)k\pi}{2(N/2)} \right\} \\
 &= \sqrt{\frac{1}{2}} [Y_k + (-1)^k Z_k] \\
 &= \sqrt{\frac{1}{2}} [Y_k + Z'_k] \quad - \quad k = 0, 1, \dots, (N/2) - 1.
 \end{aligned}$$

and the odd coefficients $R_k = X_{2k+1}$ as

$$R_k = R'_k - R_{k-1}$$

where

$$\begin{aligned}
 R'_k &= \sqrt{\frac{2}{N}} \left\{ \sum_{n=0}^{N-1} x_n \cos \frac{(2n+1)(2k+1)\pi}{2N} + \sum_{n=0}^{N-1} x_n \cos \frac{(2n+1)(2k-1)\pi}{2N} \right\} \\
 &= \frac{1}{\varepsilon_k} \sqrt{\frac{1}{2}} \left\{ \sqrt{\frac{2}{N/2}} \varepsilon_k \sum_{n=0}^{\frac{N}{2}-1} (y_n - z'_n) 2 \cos \frac{(2n+1)\pi}{2N} \cos \frac{(2n+1)k\pi}{2(N/2)} \right\} \\
 &= \frac{1}{\varepsilon_k} \sqrt{\frac{1}{2}} \left\{ \sqrt{\frac{2}{N/2}} \varepsilon_k \sum_{n=0}^{\frac{N}{2}-1} r_n \cos \frac{(2n+1)k\pi}{2(N/2)} \right\}
 \end{aligned}$$

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could

or

$$= \frac{1}{\varepsilon_k} \sqrt{\frac{1}{2}} \{ \text{length-}N/2 \text{ DCT-II of } r_n \}$$

where

$$\begin{aligned}
 r_n &= (y_n - z'_n) 2 \cos \frac{(2n+1)\pi}{2N} \\
 &= \left\{ \sqrt{\frac{2}{N/2}} \sum_{l=0}^{\frac{N}{2}-1} \varepsilon_l Y_l \cos \frac{(2n+1)l\pi}{2(N/2)} - \sqrt{\frac{2}{N/2}} \sum_{l=0}^{\frac{N}{2}-1} \varepsilon_l Z'_l \cos \frac{(2n+1)l\pi}{2(N/2)} \right\} 2 \cos \frac{(2n+1)\pi}{2N} \\
 &= \left\{ \sqrt{\frac{2}{N/2}} \sum_{l=0}^{\frac{N}{2}-1} \varepsilon_l (Y_l - Z'_l) \cos \frac{(2n+1)l\pi}{2(N/2)} \right\} 2 \cos \frac{(2n+1)\pi}{2N} \\
 &= g_n 2 \cos \frac{(2n+1)\pi}{2N}
 \end{aligned}$$

where

g_n is a length- $N/2$ IDCT of $(Y_l - Z'_l)$, and where

$$R'_k = X_{2k+1} + X_{2k+1}$$

or as

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$$\begin{aligned}
X_{2k} &= \sqrt{\frac{2}{N}} \varepsilon_{2k} \sum_{n=0}^{N-1} x_n \cos \frac{(2n+1)2k\pi}{2N} \\
&= \sqrt{\frac{2}{N}} \varepsilon_k \left\{ \sum_{n=0}^{\frac{N-1}{2}} x_n \cos \frac{(2n+1)k\pi}{2(N/2)} + \sum_{n=N/2}^{N-1} x_n \cos \frac{(2n+1)k\pi}{2(N/2)} \right\} \\
&= \sqrt{\frac{2}{N}} \varepsilon_k \left\{ \sum_{n=0}^{\frac{N-1}{2}} y_n \cos \frac{(2n+1)k\pi}{2(N/2)} + \sum_{n=0}^{\frac{N-1}{2}} x_{N-1-n} \cos \left[\frac{[2(N-1-n)+1]k\pi}{2(N/2)} \right] \right\} \\
&= \sqrt{\frac{1}{2}} \left\{ \sqrt{\frac{2}{N/2}} \varepsilon_k \sum_{n=0}^{\frac{N-1}{2}} y_n \cos \frac{(2n+1)k\pi}{2(N/2)} + \sqrt{\frac{2}{N/2}} \varepsilon_k \sum_{n=0}^{\frac{N-1}{2}} z_n \cos \frac{(2n+1)k\pi}{2(N/2)} \right\} \\
&= \sqrt{\frac{1}{2}} [Y_k + (-1)^k Z_k] \\
&= \sqrt{\frac{1}{2}} [Y_k + Z'_k] \quad k = 0, 1, \dots, (N/2) - 1.
\end{aligned}$$

and the odd coefficients $R_k = X_{2k+1}$ as

$$R_k = R'_k - R_{k-1}$$

where

$$\begin{aligned}
R_k &= \sqrt{\frac{2}{N}} \left\{ \sum_{n=0}^{N-1} x_n \cos \frac{(2n+1)(2k+1)\pi}{2N} + \sum_{n=0}^{N-1} x_n \cos \frac{(2n+1)(2k-1)\pi}{2N} \right\} \\
&= \frac{1}{\varepsilon_k} \sqrt{\frac{1}{2}} \left\{ \sqrt{\frac{2}{N/2}} \varepsilon_k \sum_{n=0}^{\frac{N-1}{2}} (y_n - z'_n) 2 \cos \frac{(2n+1)\pi}{2N} \cos \frac{(2n+1)k\pi}{2(N/2)} \right\} \\
&= \frac{1}{\varepsilon_k} \sqrt{\frac{1}{2}} \left\{ \sqrt{\frac{2}{N/2}} \varepsilon_k \sum_{n=0}^{\frac{N-1}{2}} r_n \cos \frac{(2n+1)k\pi}{2(N/2)} \right\}
\end{aligned}$$

or

$$= \frac{1}{\varepsilon_k} \sqrt{\frac{1}{2}} \{ \text{length-}N/2 \text{ DCT-II of } r_n \}$$

where

$$\begin{aligned}
 r_n &= (y_n - z'_n) 2 \cos \frac{(2n+1)\pi}{2N} \\
 &= \left\{ \sqrt{\frac{2}{N/2}} \sum_{i=0}^{N/2-1} \varepsilon_i Y_i \cos \frac{(2n+1)i\pi}{2(N/2)} - \sqrt{\frac{2}{N/2}} \sum_{i=0}^{N/2-1} \varepsilon_i Z'_i \cos \frac{(2n+1)i\pi}{2(N/2)} \right\} 2 \cos \frac{(2n+1)\pi}{2N} \\
 &= \left\{ \sqrt{\frac{2}{N/2}} \sum_{i=0}^{N/2-1} \varepsilon_i (Y_i - Z'_i) \cos \frac{(2n+1)i\pi}{2(N/2)} \right\} 2 \cos \frac{(2n+1)\pi}{2N} \\
 &= g_n 2 \cos \frac{(2n+1)\pi}{2N}
 \end{aligned}$$

where

g_n is a length- $N/2$ IDCT of $(Y_i - Z'_i)$, and where

$$R'_k = X_{2k+1} + X_{2k-1}$$

or as

$$\begin{aligned}
 X_{2k+1} &= \sqrt{\frac{2}{N}} \varepsilon_{2k+1} \sum_{i=0}^{N-1} x_i \cos \frac{(2i+1)(2k+1)\pi}{2N} \\
 &= \sqrt{\frac{2}{N}} \left\{ \sum_{i=0}^{N/2-1} x_i \cos \frac{(2i+1)(2k+1)\pi}{2N} + \sum_{i=0}^{N/2-1} x_{i+N/2} \cos \frac{(2i+N+1)(2k+1)\pi}{2N} \right\} \\
 &= \sqrt{\frac{2}{N}} \left\{ \sum_{i=0}^{N/2-1} y_i \cos \frac{(2i+1)(2k+1)\pi}{2N} + \sum_{i=0}^{N/2-1} z_i \cos \left[\frac{(2i+1)(2k+1)\pi}{2N} + (k\pi + \frac{\pi}{2}) \right] \right\} \\
 &= \sqrt{\frac{2}{N}} \left\{ \sum_{i=0}^{N/2-1} y_i \cos \frac{(2i+1)(2k+1)\pi}{2N} + (-1)^{k+1} \sum_{i=0}^{N/2-1} z_i \sin \frac{(2i+1)(2k+1)\pi}{2N} \right\} \\
 &= \sqrt{\frac{2}{N}} (X1_k - (-1)^k X2_k), \quad k = 0, 1, \dots, (N/2) - 1.
 \end{aligned}$$

SUB A2)

8. A decoder according to any of claims 5 - 7, characterised in that N is equal to 2^m , m being a positive integer > 0
9. A transcoder comprising an encoder or decoder according to any of claims 1 - 8.
10. A system for transmitting DCT transformed image or video data comprising an encoder or decoder according to any of claims 1 - 8.

Sub B 11. A method of encoding an image in the compressed (DCT) domain, using DCTs of lengths $N/2$ and wherein the compressed frames are undersampled by a certain factor in each dimension, **characterised in that** an $N \times N$ DCT is directly calculated from 4 adjacent $N/2 \times N/2$ blocks of DCT coefficients of the incoming compressed frames, N being a positive, even integer.

12. A method of encoding an image represented as a DCT transformed sequence of length N , N being a positive, even integer, **characterised in that** the DCT is calculated directly from two sequences of length $N/2$ representing the first and second half of the original sequence of length N .

A 13. A method according to ^{claim 11} any of claims 11 or 12, **characterised in that** the even coefficients of a DCT of length N are calculated as:

$$\begin{aligned}
 X_{2k} &= \sqrt{\frac{2}{N}} \varepsilon_{2k} \sum_{n=0}^{N-1} x_n \cos \frac{(2n+1)2k\pi}{2N} \\
 &= \sqrt{\frac{2}{N}} \varepsilon_k \left\{ \sum_{n=0}^{\frac{N}{2}-1} x_n \cos \frac{(2n+1)k\pi}{2(N/2)} + \sum_{n=N/2}^{N-1} x_n \cos \frac{(2n+1)k\pi}{2(N/2)} \right\} \\
 &= \sqrt{\frac{2}{N}} \varepsilon_k \left\{ \sum_{n=0}^{\frac{N}{2}-1} y_n \cos \frac{(2n+1)k\pi}{2(N/2)} + \sum_{n=0}^{\frac{N}{2}-1} x_{N-1-n} \cos \left[\frac{[2(N-1-n)+1]k\pi}{2(N/2)} \right] \right\} \\
 &= \sqrt{\frac{1}{2}} \left\{ \sqrt{\frac{2}{N/2}} \varepsilon_k \sum_{n=0}^{\frac{N}{2}-1} y_n \cos \frac{(2n+1)k\pi}{2(N/2)} + \sqrt{\frac{2}{N/2}} \varepsilon_k \sum_{n=0}^{\frac{N}{2}-1} z_n \cos \frac{(2n+1)k\pi}{2(N/2)} \right\} \\
 &= \sqrt{\frac{1}{2}} [Y_k + (-1)^k Z_k] \\
 &= \sqrt{\frac{1}{2}} [Y_k + Z'_k] \quad k = 0, 1, \dots, (N/2) - 1.
 \end{aligned}$$

and the odd coefficients $R_k = X_{2k+1}$ as

$$R_k = R'_k - R_{k-1}$$

where

$$R'_k = \sqrt{\frac{2}{N}} \left\{ \sum_{n=0}^{N-1} x_n \cos \frac{(2n+1)(2k+1)\pi}{2N} + \sum_{n=0}^{N-1} x_n \cos \frac{(2n+1)(2k-1)\pi}{2N} \right\}$$

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$$\begin{aligned}
 X_{2k+1} &= \sqrt{\frac{2}{N}} \varepsilon_{2k+1} \sum_{i=0}^{N-1} x_i \cos \frac{(2i+1)(2k+1)\pi}{2N} \\
 &= \sqrt{\frac{2}{N}} \left\{ \sum_{i=0}^{\frac{N}{2}-1} x_i \cos \frac{(2i+1)(2k+1)\pi}{2N} + \sum_{i=0}^{\frac{N}{2}-1} x_{i+N/2} \cos \frac{(2i+N+1)(2k+1)\pi}{2N} \right\} \\
 &= \sqrt{\frac{2}{N}} \left\{ \sum_{i=0}^{\frac{N}{2}-1} y_i \cos \frac{(2i+1)(2k+1)\pi}{2N} + \sum_{i=0}^{\frac{N}{2}-1} z_i \cos \left[\frac{(2i+1)(2k+1)\pi}{2N} + \left(k\pi + \frac{\pi}{2}\right) \right] \right\} \\
 &= \sqrt{\frac{2}{N}} \left\{ \sum_{i=0}^{\frac{N}{2}-1} y_i \cos \frac{(2i+1)(2k+1)\pi}{2N} + (-1)^{k+1} \sum_{i=0}^{\frac{N}{2}-1} z_i \sin \frac{(2i+1)(2k+1)\pi}{2N} \right\} \\
 &= \sqrt{\frac{2}{N}} (X1_k - (-1)^k X2_k), \quad k = 0, 1, \dots, (N/2) - 1.
 \end{aligned}$$

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SUB A3) 14. A method according to any of claims 11 - 13, characterised in that N is equal to 2^m , m being a positive integer > 0

Sub B8 15. A method of decoding an image represented as a DCT transformed sequence of length N, N being a positive, even integer, characterised in that the DCT is calculated directly from two sequences of length N/2 representing the first and second half of the original sequence of length N.

16. A method of decoding an image in the compressed (DCT) domain, using DCTs of lengths N/2 and wherein the compressed frames are undersampled by a certain factor in each dimension, characterised in that an NxN DCT is directly calculated from 4 adjacent N/2xN/2 blocks of DCT coefficients of the incoming compressed frames, N being a positive, even integer.

A *claim 15* 17. A method according to any of claims 15 or 16, characterised in that the even coefficients of a DCT of length N are calculated as:

$$\begin{aligned}
X_{2k} &= \sqrt{\frac{2}{N}} \varepsilon_{2k} \sum_{n=0}^{N-1} x_n \cos \frac{(2n+1)2k\pi}{2N} \\
&= \sqrt{\frac{2}{N}} \varepsilon_k \left\{ \sum_{n=0}^{N/2-1} x_n \cos \frac{(2n+1)k\pi}{2(N/2)} + \sum_{n=N/2}^{N-1} x_n \cos \frac{(2n+1)k\pi}{2(N/2)} \right\} \\
&= \sqrt{\frac{2}{N}} \varepsilon_k \left\{ \sum_{n=0}^{N/2-1} y_n \cos \frac{(2n+1)k\pi}{2(N/2)} + \sum_{n=0}^{N/2-1} x_{N-1-n} \cos \left[\frac{[2(N-1-n)+1]k\pi}{2(N/2)} \right] \right\} \\
&= \sqrt{\frac{1}{2}} \left\{ \sqrt{\frac{2}{N/2}} \varepsilon_k \sum_{n=0}^{N/2-1} y_n \cos \frac{(2n+1)k\pi}{2(N/2)} + \sqrt{\frac{2}{N/2}} \varepsilon_k \sum_{n=0}^{N/2-1} z_n \cos \frac{(2n+1)k\pi}{2(N/2)} \right\} \\
&= \sqrt{\frac{1}{2}} [Y_k + (-1)^k Z_k] \\
&= \sqrt{\frac{1}{2}} [Y_k + Z'_k] \quad k = 0, 1, \dots, (N/2) - 1.
\end{aligned}$$

and the odd coefficients $R_k = X_{2k+1}$ as

$$R_k = R'_k - R_{k-1}$$

where

$$\begin{aligned}
R'_k &= \sqrt{\frac{2}{N}} \left\{ \sum_{n=0}^{N-1} x_n \cos \frac{(2n+1)(2k+1)\pi}{2N} + \sum_{n=0}^{N-1} x_n \cos \frac{(2n+1)(2k-1)\pi}{2N} \right\} \\
&= \frac{1}{\varepsilon_k} \sqrt{\frac{1}{2}} \left\{ \sqrt{\frac{2}{N/2}} \varepsilon_k \sum_{n=0}^{N/2-1} (y_n - z'_n) 2 \cos \frac{(2n+1)\pi}{2N} \cos \frac{(2n+1)k\pi}{2(N/2)} \right\} \\
&= \frac{1}{\varepsilon_k} \sqrt{\frac{1}{2}} \left\{ \sqrt{\frac{2}{N/2}} \varepsilon_k \sum_{n=0}^{N/2-1} r_n \cos \frac{(2n+1)k\pi}{2(N/2)} \right\}
\end{aligned}$$

or

$$= \frac{1}{\varepsilon_k} \sqrt{\frac{1}{2}} \{ \text{length-}N/2 \text{ DCT-II of } r_n \}$$

where

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contd

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$$\begin{aligned}
 r_n &= (y_n - z'_n) 2 \cos \frac{(2n+1)\pi}{2N} \\
 &= \left\{ \sqrt{\frac{2}{N/2}} \sum_{i=0}^{N/2-1} \varepsilon_i Y_i \cos \frac{(2n+1)l\pi}{2(N/2)} - \sqrt{\frac{2}{N/2}} \sum_{i=0}^{N/2-1} \varepsilon_i Z'_i \cos \frac{(2n+1)l\pi}{2(N/2)} \right\} 2 \cos \frac{(2n+1)\pi}{2N} \\
 &= \left\{ \sqrt{\frac{2}{N/2}} \sum_{i=0}^{N/2-1} \varepsilon_i (Y_i - Z'_i) \cos \frac{(2n+1)l\pi}{2(N/2)} \right\} 2 \cos \frac{(2n+1)\pi}{2N} \\
 &= g_n 2 \cos \frac{(2n+1)\pi}{2N}
 \end{aligned}$$

where

g_n is a length- $N/2$ IDCT of $(Y_i - Z'_i)$, and where

$$R'_k = X_{2k+1} + X_{2k-1}.$$

or as

$$\begin{aligned}
 X_{2k+1} &= \sqrt{\frac{2}{N}} \varepsilon_{2k+1} \sum_{i=0}^{N-1} x_i \cos \frac{(2i+1)(2k+1)\pi}{2N} \\
 &= \sqrt{\frac{2}{N}} \left\{ \sum_{i=0}^{N/2-1} x_i \cos \frac{(2i+1)(2k+1)\pi}{2N} + \sum_{i=0}^{N/2-1} x_{i+N/2} \cos \frac{(2i+N+1)(2k+1)\pi}{2N} \right\} \\
 &= \sqrt{\frac{2}{N}} \left\{ \sum_{i=0}^{N/2-1} y_i \cos \frac{(2i+1)(2k+1)\pi}{2N} + \sum_{i=0}^{N/2-1} z_i \cos \left[\frac{(2i+1)(2k+1)\pi}{2N} + (k\pi + \frac{\pi}{2}) \right] \right\} \\
 &= \sqrt{\frac{2}{N}} \left\{ \sum_{i=0}^{N/2-1} y_i \cos \frac{(2i+1)(2k+1)\pi}{2N} + (-1)^{k+1} \sum_{i=0}^{N/2-1} z_i \sin \frac{(2i+1)(2k+1)\pi}{2N} \right\} \\
 &= \sqrt{\frac{2}{N}} (X1_k - (-1)^k X2_k), \quad k = 0, 1, \dots, (N/2) - 1.
 \end{aligned}$$

*B8
cancel.*

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SUB A4) 18. A method according to any of claims 15 - 17, characterised in that N is equal to 2^m , m being a positive integer > 0 .

Sub B10 19. A method of transcoding an image in the compressed (DCT) domain, using DCTs of lengths $N/2$ and wherein the compressed frames are undersampled by a certain factor in each dimension, characterised in that an $N \times N$ DCT is directly calculated from 4 adjacent $N/2 \times N/2$ blocks of DCT coefficients of the incoming compressed frames, N being a positive, even integer.

20. An encoder comprising means for performing DCT transformation of a sequence of length $N/2$, N being a positive, even integer,

characterised by

- means for calculating the DCT of length N directly from two sequences of length $N/2$ representing the first and second half of an original sequence of length $N/2$ only using DCTs of length $N/2$.

21. A method of encoding an image represented as a sequence of length N , N being a positive, even integer,

characterised in

that the DCT of length N is calculated directly from two sequences of length $N/2$ representing the first and second half of an original sequence of length N only using DCTs of length $N/2$.

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cancel.*

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